Textures and Texture Synthesis

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Outline

- motivation
- textures
- bidirectional texture function
- texture synthesis, texture generating
- texture synthesis algorithms
- BTF roller

Motivation

- to enhance realism in virtual scene
 - textures, bump maps, BTF
- texture mapping
 - an efficient way to include detail on the surfaces of objects in the scene
 - smaller texture than object surface to be covered
 - larger texture
 - tiling
 - texture synthesis

Image Texture

Texture is a structure which is made of a large ensemble of elements that resemble each other "very much", with some kind of an "order" in their locations, so that there is no one element which attracts the viewer's eye in any special way. The human viewer gets an impression of uniformity when he looks at a "**texture**".

Textures and BTF Textures



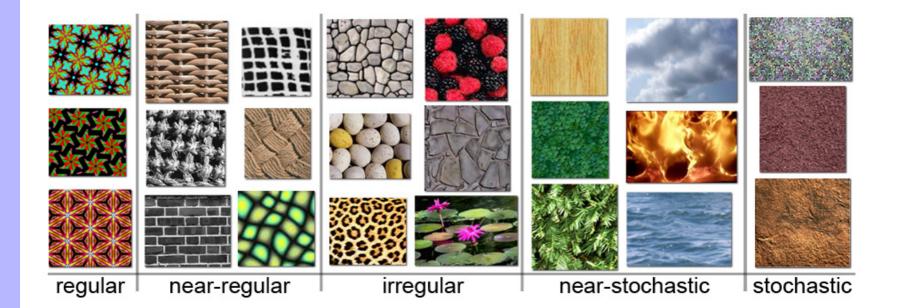
Image Texture

- there is no definition of texture
- properties
 - set of elements
 - homogenity, uniformity

Texture Categorization

- origin artificial, natural
- spectral mono-spectral, multi-spectral
- time dependence static, dynamic
- surface smooth, rough

Texture Types



Bidirectional Texture Function

- view and illumination angle dependent
- realistic appearance



Bidirectional Texture Function

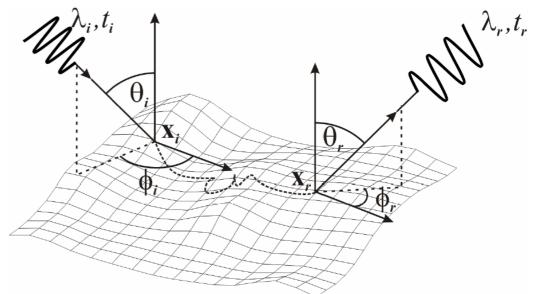


Acquisition of BTF

- 2D texture
 - simple process 2D scanner, digital camera
- BTF texture
 - complex and controlled measurement environment
 - physical measurement of real-world reflection
 - device calibration, image registration

Reflectance Measurement

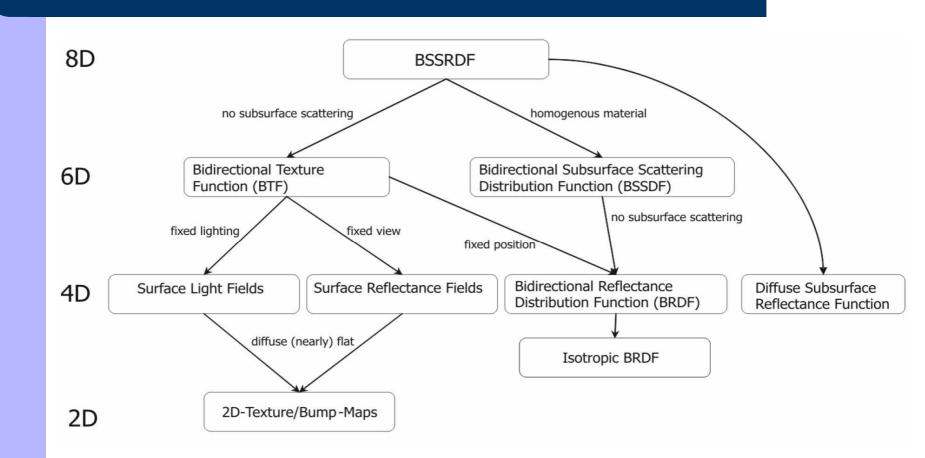
- path of photon
- parameters of general light-material interaction
- 12 parameters



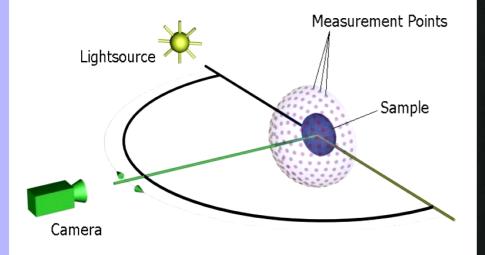
Reflectance Measurement

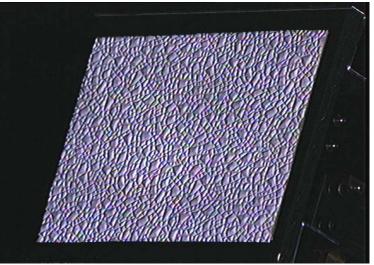
- 12 parameters \rightarrow 8 parameters
 - light transport takes zero time
 - time invariant reflectance behavior of surface
 - interaction does not change wavelength
 - wavelength \rightarrow 3 color bands, RGB
- 8D function, Bidirectional Surface Scattering Distribution Function (BSSRDF)
- BTF, BRDF, ...

Hierarchy of Reflectance Functions



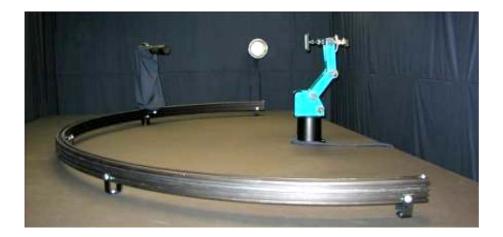
$$BTF_{RGB}(\mathbf{x},\theta_i,\phi_i,\theta_r,\phi_r) = \int_S BSSRDF_{RGB}(\mathbf{x}_i,\mathbf{x},\theta_i,\phi_i,\theta_r,\phi_r) d\mathbf{x}_i$$

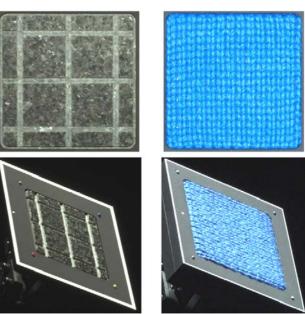




• measurement setup of the Bonn-System

 HMI lamp, CCD camera, robot with a sample holder

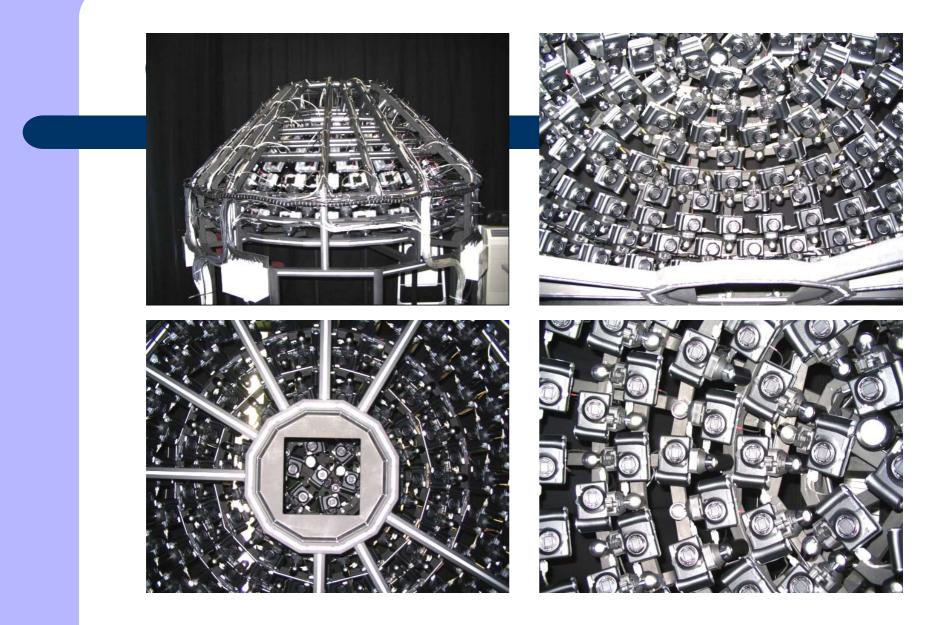




measurement setup of the Bonn-System

- 10x10 cm maximum sample size
- 81 positions for camera, 81 positions for light
- raw data 4500x3000 pixels, 12MB per image
- calibration (light-camera, aperture, geometric distortion)
- data postprocessing (rectification, registration, resize) \rightarrow 1.2GB per material

- camera array
 - fast high-quality acquisition of BTF
 - 151 digital cameras (22801 images)
 - no moving parts
 - known region of interest, no time-consuming detection of ROI
 - angular resolution 0,04161 steradians
 - spatial resolution 280DPI for BTF 1024x1024

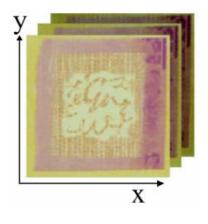


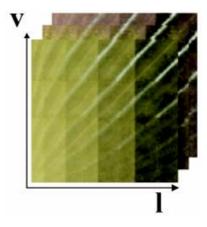
• collection of discrete textures

$$\left\{T_{(\mathbf{v},\mathbf{l})}\right\}_{(\mathbf{v},\mathbf{l})\in M}$$

 set of spatially varying apparent BRDF

$$\{B_{\mathbf{x}}\}_{\mathbf{x}\in I\subset\mathbf{N}^2}$$





- fitting analytical BRDF-models
 - Lafortune lobes

 $s(\mathbf{v},\mathbf{l}) = (\mathbf{v}^T \cdot \mathbf{M} \cdot \mathbf{l})^n$

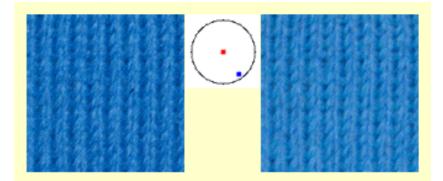
- reflectance fields

$$BTF(\mathbf{x}, \mathbf{v}, \mathbf{l}) \approx \sum_{v \in N(\mathbf{v})} w_{\mathbf{x}, v} RF_{\mathbf{x}, v}(\mathbf{l})$$
$$RF_{\mathbf{x}, v}(\mathbf{l}) \approx \rho_{d, \mathbf{x}} + \rho_{s, \mathbf{x}, v}(\mathbf{l}) \cdot \sum_{i=1}^{k} s_{\mathbf{x}, v}(\mathbf{l})$$

- fitting analytical BRDF-models
 - Lafortune lobes

$$s(\mathbf{v},\mathbf{l}) = (\mathbf{v}^T \cdot \mathbf{M} \cdot \mathbf{l})^n$$

- reflectance fields

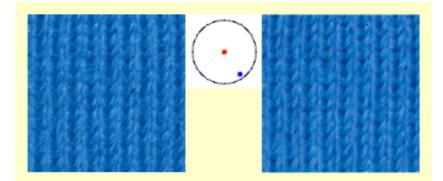


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- fitting analytical BRDF-models
 - Lafortune lobes

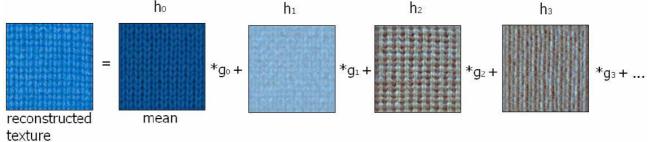
$$s(\mathbf{v},\mathbf{l}) = (\mathbf{v}^T \cdot \mathbf{M} \cdot \mathbf{l})^n$$

- reflectance fields



$$BTF(\mathbf{x}, \mathbf{v}, \mathbf{l}) \approx \sum_{v \in N(\mathbf{v})} w_{\mathbf{x}, v} RF_{\mathbf{x}, v}(\mathbf{l})$$
$$RF_{\mathbf{x}, v}(\mathbf{l}) \approx \rho_{d, \mathbf{x}} + \rho_{s, \mathbf{x}, v}(\mathbf{l}) \cdot \sum_{i=1}^{k} s_{\mathbf{x}, v}(\mathbf{l})$$

- linear basis decomposition (PCA)
 - per-texel matrix factorization $B_{\mathbf{x}}(\mathbf{v},\mathbf{l}) \approx \sum_{k=1}^{c} g_{\mathbf{x},j}(\pi_1(\mathbf{v},\mathbf{l}))h_{\mathbf{x},j}(\pi_2(\mathbf{v},\mathbf{l}))$
 - full BTF-matrix factorization $BTF(\mathbf{x}, \mathbf{v}, \mathbf{l}) \approx \sum_{j}^{c} g_{j}(\mathbf{x}) h_{j}(\mathbf{v}, \mathbf{l})$
 - per-view factorization



BTF Rendering

• rendering

$$L_r(\mathbf{x}, \mathbf{v}) = \int_{\Omega_i} \rho_{\mathbf{x}}(\mathbf{v}, \mathbf{l}) L_i(\mathbf{x}, \mathbf{l}) (n_{\mathbf{x}} \cdot \mathbf{l}) d\mathbf{l}$$

- rendering including measured BTF $L_r(\mathbf{x}, \mathbf{v}) = \int_{\Omega_i} BTF(\mathbf{x}, \mathbf{v}, \mathbf{l}) L_i(\mathbf{x}, \mathbf{l}) (n_{\mathbf{x}} \cdot \mathbf{l}) d\mathbf{l}$
 - x is simply looked up from the BTF
 - assumption: mapping from 3D-surface to 2D spatial texture domain exists



Texture Synthesis



Texture Generating

- goal: generate texture of arbitrary size
- texture modelling, mathematical modelling
 - procedural texture modelling
 - adaptive texture models
- texture sampling
 - generating from a given texture sample

Procedural Textures

- analytical scalar function of (x,y,z) coordinates
- texturing evaluation of function on object surface
 - ray-tracing 3D intersection point with surface
- textures of natural objects
 - similarity between different patches
 - repetitiveness, coherence
 - similarity on different resolution scales
 - not completely identical
 - additional disturbances, turbulence, noise
- mimics statistical properties of natural textures
- empirical approach

Examples of Procedural Textures

• marble

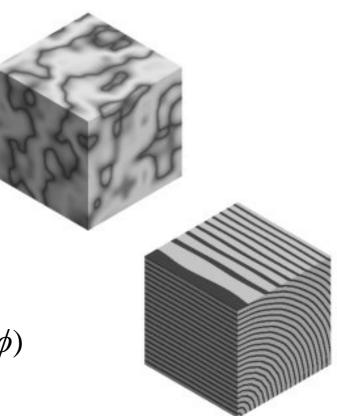
$$f(x, y, z) = \sin^n(x + t(x, y, z))$$

• wood

$$f(x, y, z) = x^{2} + y^{2} + n(x, y, z)$$

- clouds $f(x, y, z) = \sum_{i=1}^{4} 2^{-i} n(2^{i} x, 2^{i} y, 2^{i} z)$ • fire
- fire

$$f(x, y, z) = z + \sum_{i=1}^{4} 2^{-i} n(2^{i} x, 0, 2^{i} z + \phi)$$

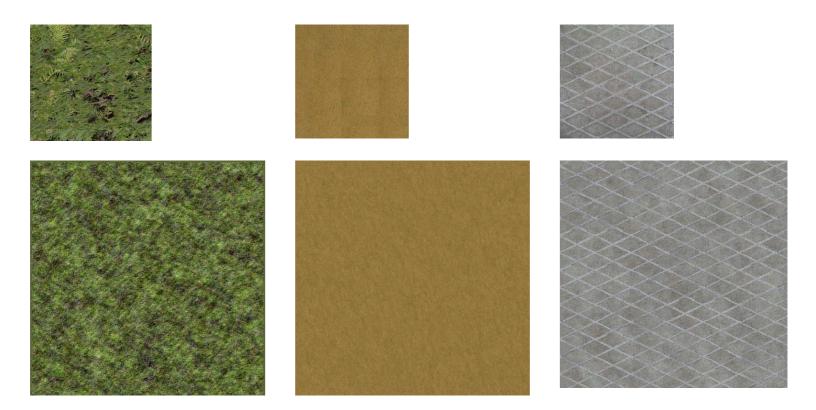


Adaptive Texture Models

- procedural form
- Gaussian Markov Random Fields
 - flexible for natural or artificial texture simulation
 - represents high frequencies well
- extreme compression only few parameters have to be stored
- unknown relation between parameters and visual appearance of texture

Adaptive Texture Models Results

• 3D Causal Autoregressive Model



Sampling-based Texture Synthesis

• given a small texture patch, fill an arbitrary region

- tiling
 - discontinuities along edges?
 - artificial appearance completely regular





Sampling Versus Modelling

- sampling
 - given texture
 - realistic synthetic texture
 - limited resolution, aliasing
 - high memory consumption
- adaptive models
 - procedural form

- modelling
 - unlimited resolution
 - low memory consumption
 - cannot model given texture
 - unknown relation between parameters and texture appearance

Sampling-based Texture Synthesis

- given texture *I*, generate a texture *J* which
 - looks like the same texture
 - has no obvious copying or tiling from I
 - difference between *I* and *J* should be the same as *I* "differs from itself"
- intelligent sampling approaches
 - preserve stochastic properties, no regularity (tiling), no visible seams
 - analytical part, synthesis part
 - not separated, partially separated of fully separated
 - if separated, real-time synthesis is possible

Intelligent Sampling Approaches

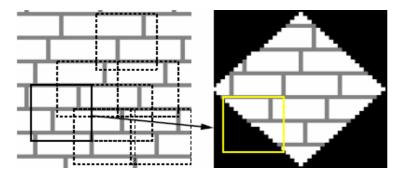
- different approaches
 - multiresolution pyramids
 - pixel-by-pixel synthesis
 - multiresolution pixel-by-pixel
 - patch-based synthesis
 - advanced tiling techniques
- no universal method exists
 - stochastic textures
 - near-periodic textures
 - BTF textures

Texture Synthesis Algorithms



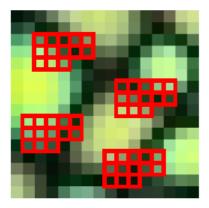
Non-parametric Sampling

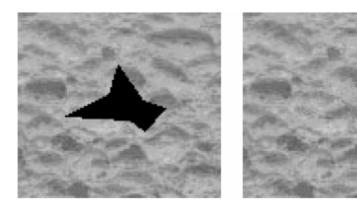
- Efros, Leung, 1999
- properties
 - MRF: probability of synthesized pixel depends on its neighborhood; independent of the rest of image
 - neighborhood
 - square window, size of window free parameter
 - causal



Non-parametric Sampling

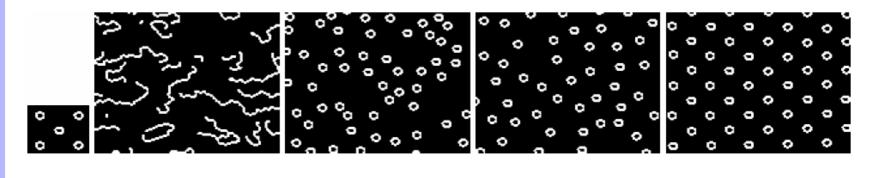
- neighborhood distance: d=d_{SSD}*G
- possible pixels: dist< $(1+\epsilon)^*d(N,N_{best})$
- synthesis: outward from 3-by-3 seed randomly taken from input sample
- hole filling: from the edges of the hole

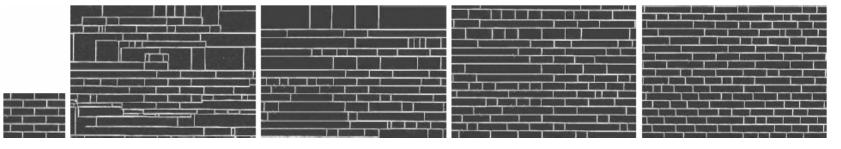




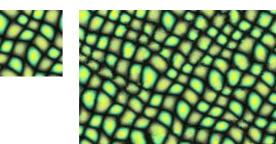
Non-parametric Sampling Results

• size of neighborhood – 5, 11, 15, 23 pixels





Non-parametric Sampling Results







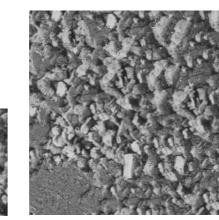
ut it becomes harder to lau ound itself, at "this daily i ving rooms," as House Der iscribed it last fall. He fai uthe left a ringing question ore years of Monica Lewir inda Tripp?" That now seer ?olitical comedian Al Fran vit phase of the story will the formaction relian cooling resert, accounts of new access it ndatwears coune Tring rooms," as Heft he fast nd it l ars dat noears oortseas ribed it last n# hest bedian Al. H econicalHomd it h Al. Heft ars of as da Lewindailf l lian Al Ths," as Lewing questies last aticarsticall. He is dian Al last fal counda Lew, at "this dailyears d ily edianicall. Hoorewing rooms," as House De fale f De und itical counsestscribed it last fall. He fall. Hefft rs orcheoned it nd it he left a ringing questica Lewin . icars coecoms," astore years of Monica Lewinow seee a Thas Fring roome stooniscat nowea re left a roouse bouestof MHe lelft a Lést fast ngine làuuesticars Hef ud it rip?" TrHouself, a ringind itsonestud it a ring que: astical cois ore years of Moung fall. He ribof Mouse)re years ofanda Tripp?" That hedian Al Lest fasee yea nda Tripp?' Holitical comedian Alét he few se ring que olitical cone re years of the storears ofas l Frat nica L ras Lew se lest a rime l He fas questinging of, at beou



Non-parametric Sampling Failures

growing garbage

verbatim copying



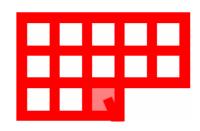


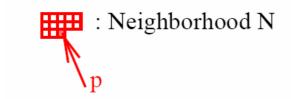


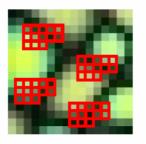
Non-parametric Sampling

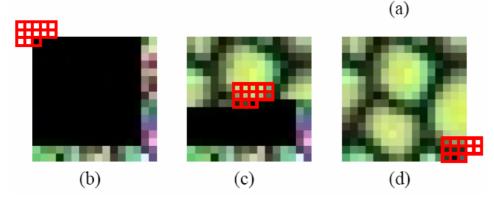
- size of neighborhood
 - largest feature size
 - the only parameter specified by user
- not separated analytical part from synthesis step
 - each pixel full search
 - k-NN search in 3*(w²/2-1) dimensions
 - very slow synthesis

- Wei, Levoy, 2001
- algorithm
 - initialize J to noise
 - synthesize new pixels in scanline order
 - select new pixel from *I* that has the closest matching neighborhood to *J*
 - in multiresolution case, look at feature vectors instead of neighborhood









- scanline synthesis with neighborhoods
 - (a) input texture
 - (b) start
 - (c) midway point
 - (d) end

• multiresolution approach

- search for X neighborhood vector is constructed from O's, Q's and Y
- small neighborhoods can be used

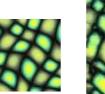
	0	0	0	0	0	
	0	0	0	0	0	
	0	0	Х			

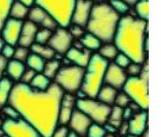
Q	Q	Q	
Q	Y	Q	
Q	Q	Q	

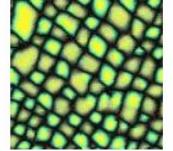


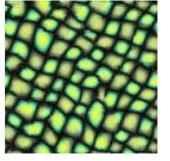
L+1

- 5x5 top level,
 - 1, 2, 3 levels



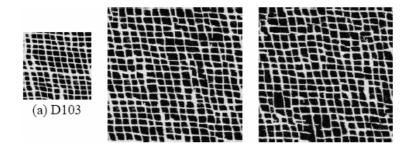


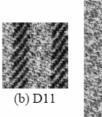


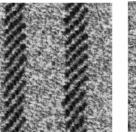


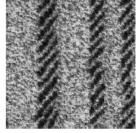
• TSVQ acceleration

- exhaustive search very slow
- N(p) point in multi-dimensional space
 - neighborhood matching = nearest point search problem
 - $\{N(p_i)\}$ from each $G_a(L)$ as the training data
 - generate tree structure codebooks
 - synthesis time complexity O(log N_L) of search
- adds additional unpredictability

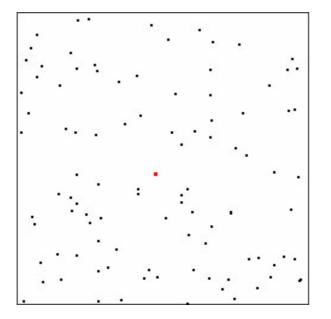


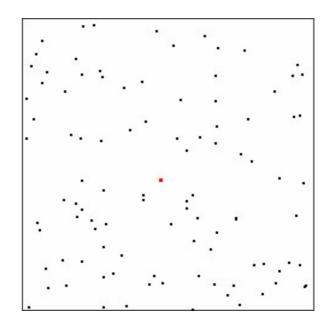




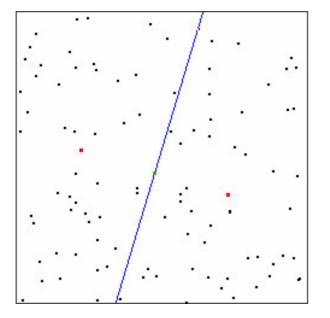


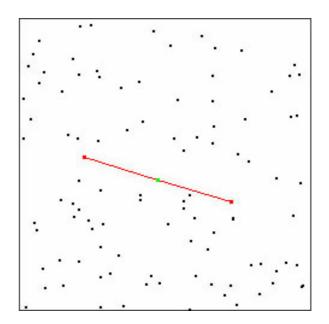
• TSVQ demonstration - initialization



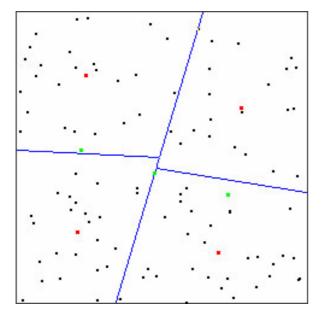


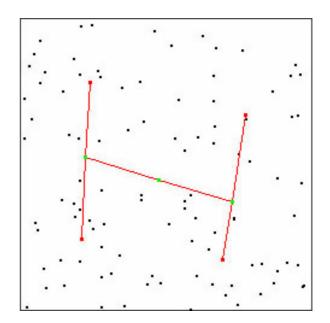
• TSVQ demonstration – 1. step



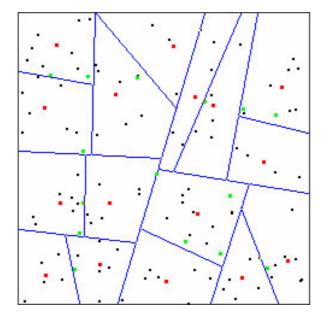


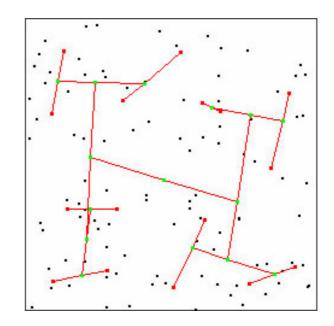
• TSVQ demonstration – 2. step



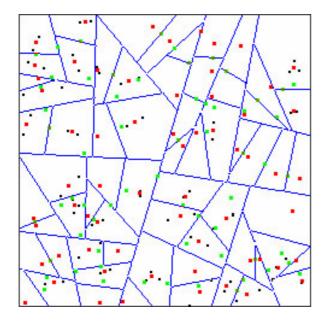


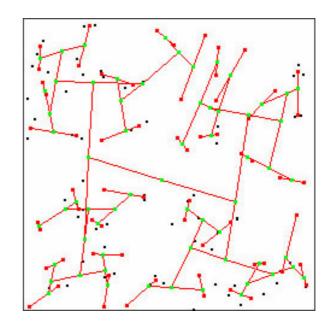
• TSVQ demonstration – 4. step



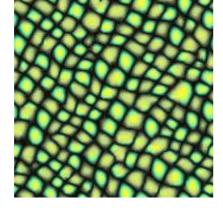


• TSVQ demonstration – 6. step















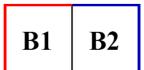






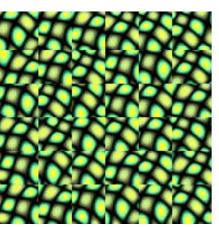
- parameters
 - neighborhood size and number of levels
 - TSVQ number of codewords
- not fully separated analytical part from synthesis step
 - analysis
 - codebook construction
 - synthesis
 - each pixel search using TSVQ logaritmic complexity
 - much faster than NPS

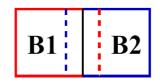
- Efros, Freeman, 2001
- complex textures very few pixels have a choice of values to assign
- pasting overlapping patches of the input texture into a rectangular grid and fixing the seams
- algorithm:
 - initialize J to empty
 - copy new patches of certain size in scanline order, with fixed overlap width
 - randomly select new patch with overlap error less than given threshold
 - crop patch by minimal error boundary cut



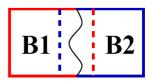


input texture random placement of blocks

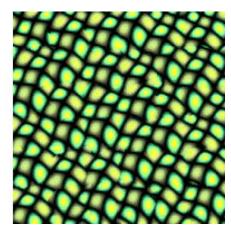




neighboring blocks constrained by overlap



minimum error boundary cut



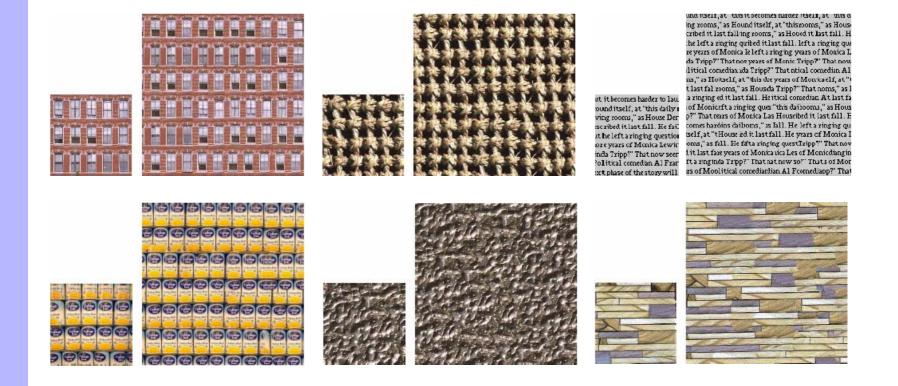
- minimum error boundary cut
 - $E_{i,j} = e_{i,j} + \min(E_{i-1,j-1}, E_{i-1,j}, E_{i-1,j+1})$
 - dynamic programming
- overlap error L2 norm on pixel values
- width of overlap 1/6 of the size of the block
- matching block tolerance within 0.1 times error of the best matching block

• demo of the method





Image Quilting Results



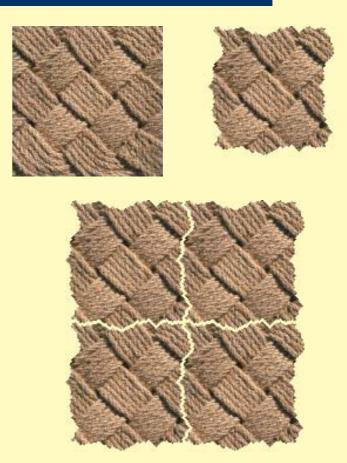
- parameters
 - size of the square block
 - width of the overlap
- not separated analytical part from synthesis step
 - exhaustive search of best patch
 - very slow
- possible improvement
 - speed search acceleration via TSVQ
 - quality A* or Dijkstra's algorithm

General Failures

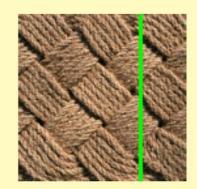
- non-uniform image intensity
 - algorithm slips into some region
- geometric distortion
 - perspective
- non-representative texture sample
 - low frequencies not captured

BTF Roller

- basic method
 - maximal toroidal tile
 - tiling
- advanced method
 - automatic tile size estimation
 - tiling of multiple tiles
 - BTF







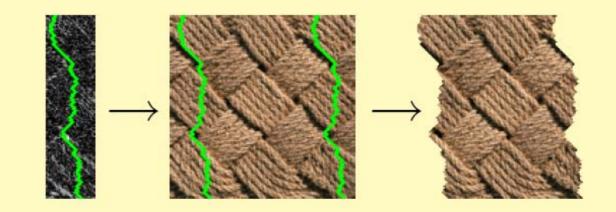




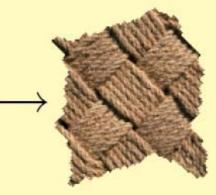




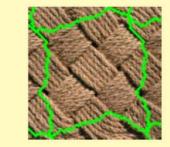
overlapoptimal cut

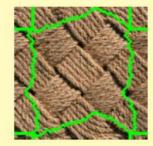


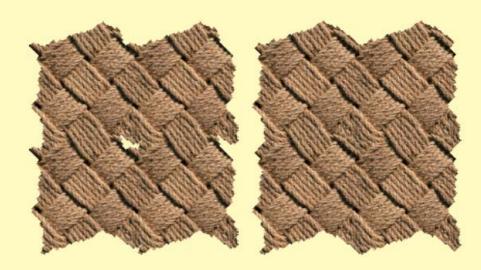




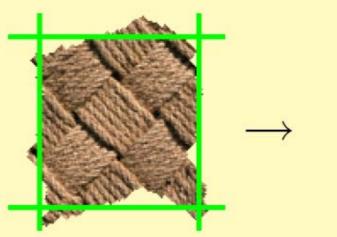
- overlap
- optimal cut
- corner treatment







- overlap
- optimal cut
- corner treatment
- rectangular tile

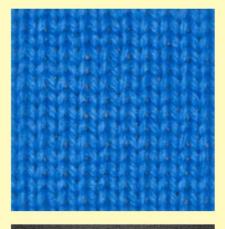




Multiple Tiles

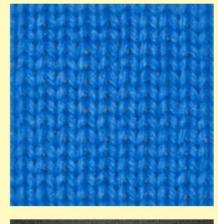
- structure of synthetic texture
 - avoid artificial regularity
 - preserve original structure
- tile filling replacement
- optimal tile size estimation
 - number of tiles k
 - frequency content

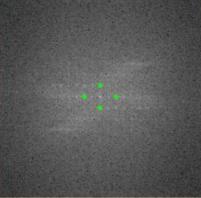
- Fourier transform
 - texture sample N × M





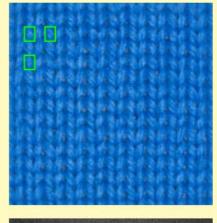
- Fourier transform
 - texture sample N × M
 - $-f_{row}, f_{col}$

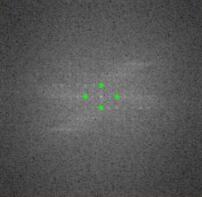




- Fourier transform
 - texture sample N × M
 - $-f_{row}, f_{col}$
- texture analysis

- n_{row} , n_{col}

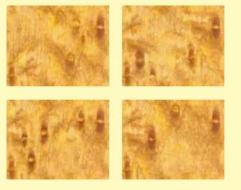




- tile $N_t \times M_t$
 - as large as possible

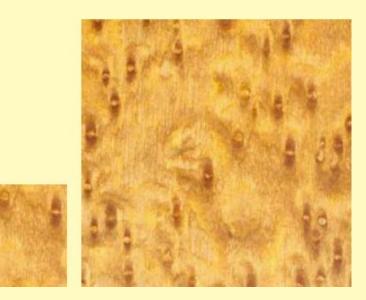
 $- N_t M_t \approx (1/k) NM$





Tile Filling Replacement

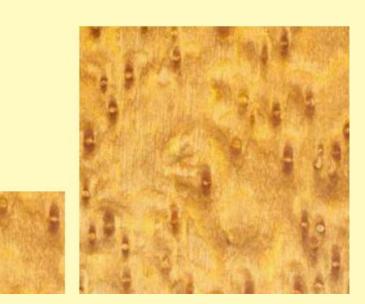
 preserve seamless elargement

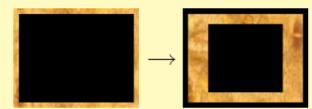




Tile Filling Replacement

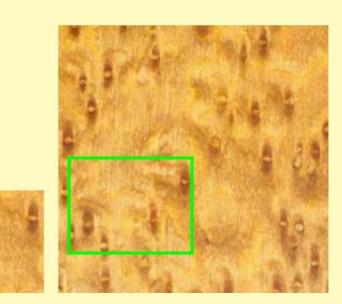
- preserve seamless elargement
- new tile filling
 - search



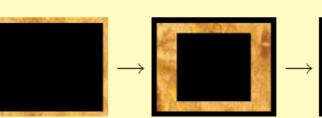


Tile Filling Replacement

- preserve seamless elargement
- new tile filling
 - search





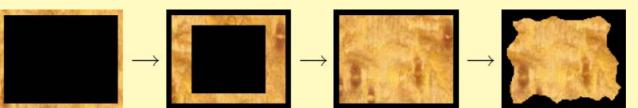




Tile Filling Replacement

- preserve seamless elargement
- new tile filling
 - search
 - crop





Tile Filling Replacement

- preserve seamless elargement
- new tile filling
 - search
 - crop
- new tile







Roller Algorithm and BTF Synthesis

smooth textures analysis

- estimates
- tile
- tile filling search
- new tiles

synthesis

BTF textures analysis

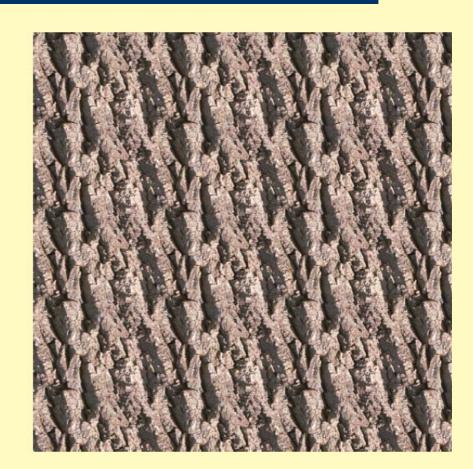
- estimates
 - perpendicular illumination
- tile
 - all illumination angles
- tile filling search
 - perpendicular illumination
- new tiles
 - all illumination angles

synthesis

Results – 1 Tile



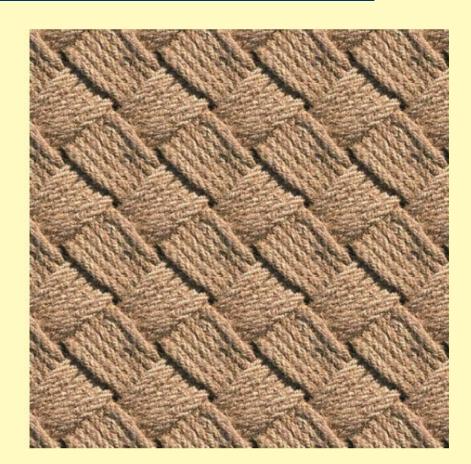




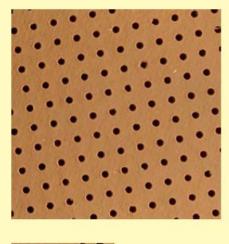
Results – 1 Tile

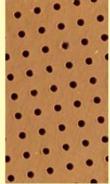


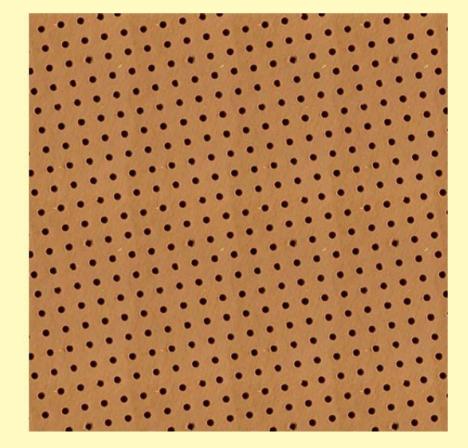




Results – 1 Tile



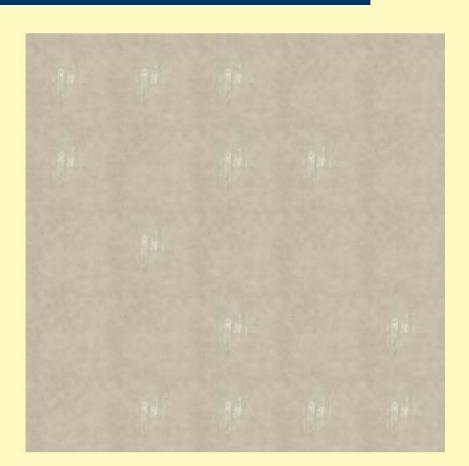




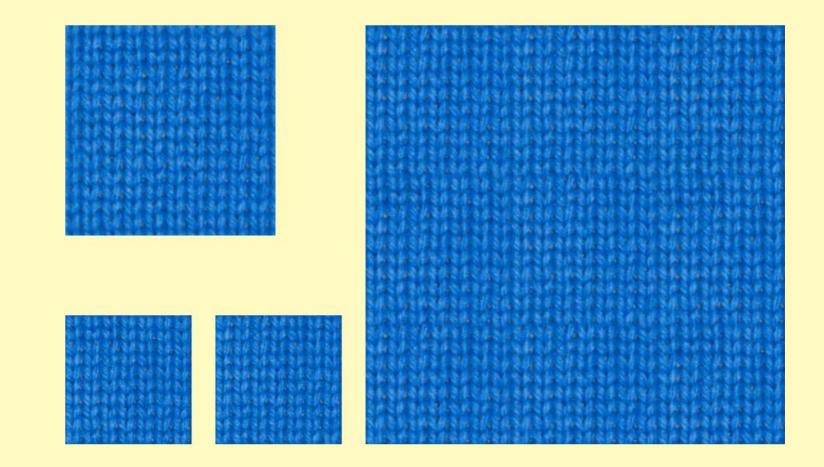
Results – 2 Tiles



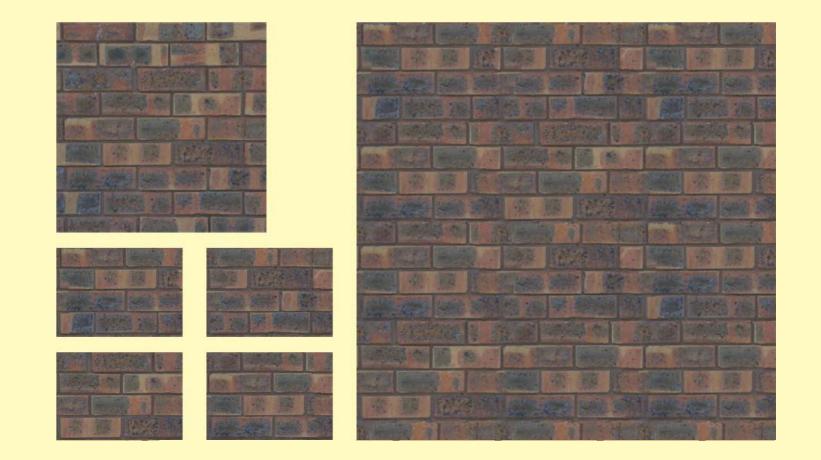




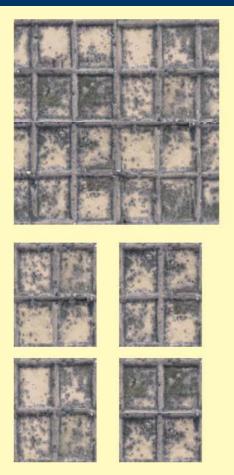
Results – 2 Tiles

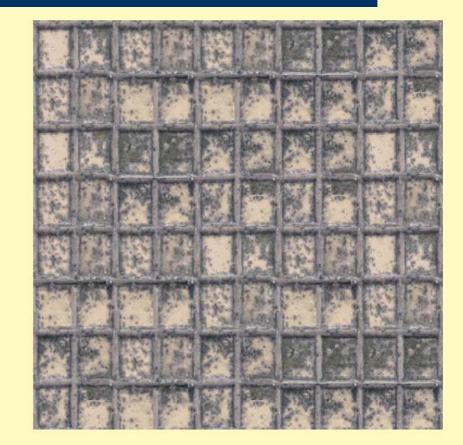


Results – 4 Tiles



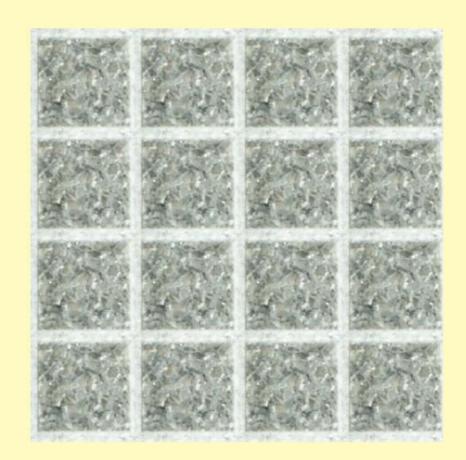
Results – 4 Tiles

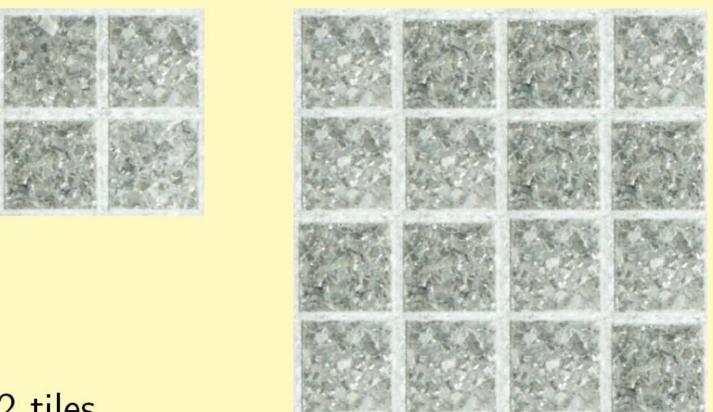




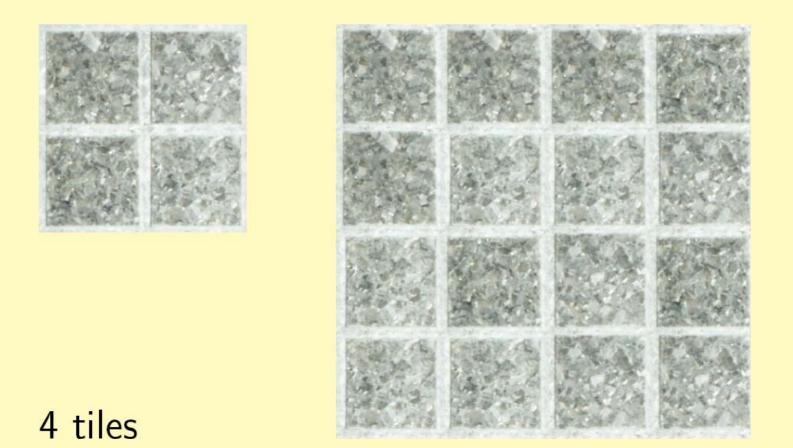


1 tile





2 tiles







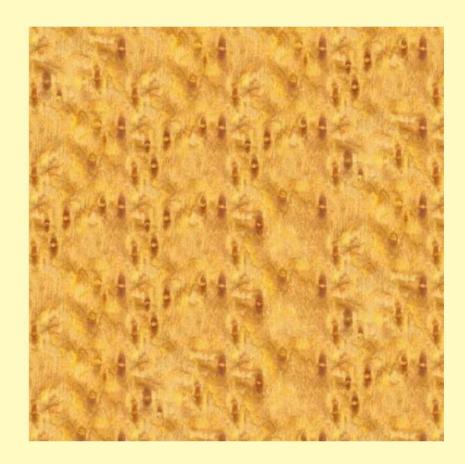
1 tile





2 tiles



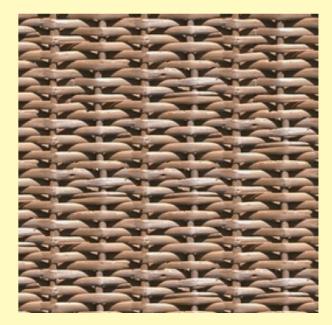


4 tiles

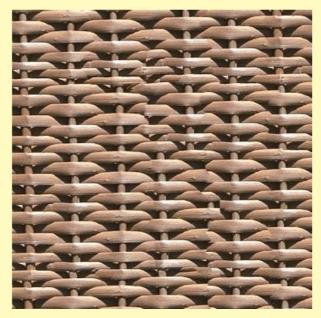
BTF Synthesis

- wool
- wood

Roller







Roller

Arrow Arrow <td< th=""><th></th><th></th><th></th><th></th><th></th><th></th><th>Caden le</th><th></th><th>Can and a state of the state of</th><th></th></td<>							Caden le		Can and a state of the state of	
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Roller

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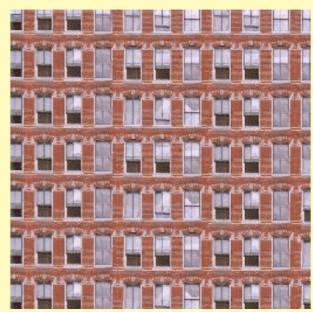
Image Quilting

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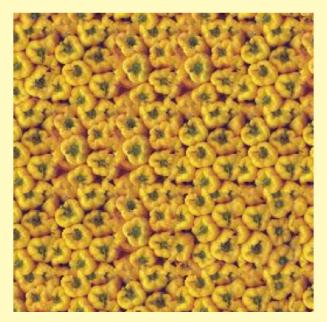
Roller







Roller







Roller







Failures

• non-uniform image intensity

Roller



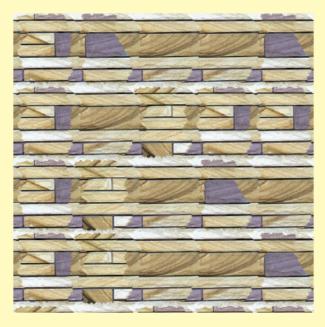




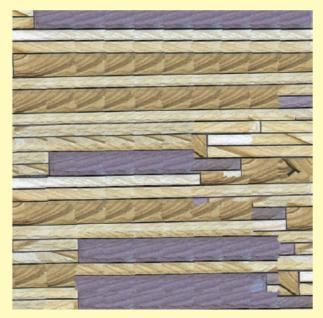
Failures

non-representative sample

Roller







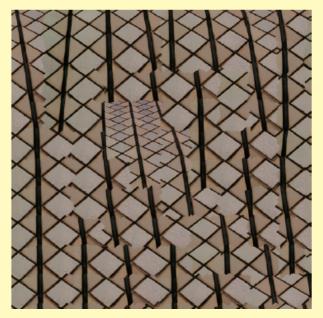
Failures

perspective distortion

Roller







Summary of Roller method

- automatic algorithm
 - the only parameter k tiles
- real-time synthesis
- analysis time consumption
 - not important
 - 256×256, 1 tile ... 36s
- very good results
- fast GPU implementation possible

Application

- smooth textures
- BTF textures
- alternative types of textures
 - eigen-textures
- parametric spaces of reflectance models